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and Set-Theoretic Topology”

dedicated to Professor A. V. Arhangel'skii's
80th birthday

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и теоретико-множественная топология»

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On embedding of spaces into Tychonoff products

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The A. V. Archangel’skiĭ theorem on the cardinality of a compact Hausdorff first countable space caused a great increase in the study of cardinal characteristics of spaces and methods of their proofs.

We consider problems of an embedding of a space X into Tychonoff products of spaces, which has some properties of projections.

Using this embedding, we study properties of the space X as a subspace of the product and prove the cardinal characteristics of X that follow from these properties.

On the classification of spaces $C_p(X)$,
where X is a countable metric space

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Our talk will be devoted to problems of uniform and linearly topological classification of spaces $C_p(X)$, where X is a countable metric space.