Toposym 2022 Book of Abstracts

A. Bartoš, D. Chodounský (eds.)



FACULTY OF MATHEMATICS AND PHYSICS Charles University



Institute of Mathematics Czech Academy of Sciences



FACULTY OF INFORMATION TECHNOLOGY CTU IN PRAGUE Faculty of Mathematics and Physics Charles University Ke Karlovu 3 121 16 Praha 2 Czech Republic

Institute of Mathematics Czech Academy of Sciences Žitná 25 115 67 Praha 1 Czech Republic

Faculty of Information Technology Czech Technical University in Prague Thákurova 9 160 00 Praha 6 Czech Republic

Published by MatfyzPress Publishing House of the Faculty of Mathematics and Physics of Charles University Sokolovská 83, 186 75 Praha 8, Czech Republic as publication number 659. Printed by Reprostředisko MFF UK.

The text has not been reviewed by the publishing house MatfyzPress. The publication has been issued for the purposes of the Toposym 2022 conference. The publishing house Matfyzpress is not responsible for the quality or content of the text.

Copyright © A. Bartoš, D. Chodounský (eds.), 2022 Copyright © Individual authors, 2022 Copyright © MatfyzPress, Publishing House of the Faculty of Mathematics and Physics of Charles University, 2022 ISBN 978-80-7378-465-2



Some rights reserved. This work is licensed under http://creativecommons.org/licenses/by-sa/3.0/



We would like to gratefully acknowledge the support of Elsevier B.V., Foundation Compositio Mathematica, the National Science Foundation, and the RSJ Foundation.

Table of contents

Preface	13
Organizers	15
Invited speakers	17
Plenary talks	19
Automatic continuity of measurable homomorphisms on Čech-complete topological groups (<i>Taras Banakh</i>)	20
S and Moore–Mrowka spaces under really not CH (Alan Dow)	20 21
Todorčević' trichotomy and a hierarchy in the class of tame dynamical systems (<i>Eli Glasner</i>)	22
Ultrafilters and countably compact groups $(Michael Hrušák)$	23
Complexity of distances, reducibility and universality (Ondřej Kurka)	24
Many weak P-sets (Jan van Mill)	25
On pseudoarc and dynamics (<i>Piotr Oprocha</i>)	26
On the problem of amenability of groups of maps (<i>Vladimir Pestov</i>)	27
Amenability, optimal transport and abstract ergodic theorems (<i>Christian Rosendal</i>)	28
On stability and weight of Lindelöf <i>P</i> -groups (<i>Mikhail Tkachenko</i>)	29

Generic metrizability (Stevo Todorčević)	30
Selection principles and omission of intervals $(Boaz \ Tsaban)$	31
Semi-plenary talks	33
Some hyperspaces of compact convex sets and their orbit spaces (Sergey Antonyan)	34
Compact spaces associated to Banach lattices (Antonio Avilés)	35
Model theory in Ramsey theory (Dana Bartošová)	36
Partitioning the real line into Borel sets (<i>Will Brian</i>)	37
Entropy of amenable monoid actions (<i>Dikran Dikranjan</i>)	38
Hyperspaces of Erdős space (Rodrigo Hernández-Gutiérrez)	39
Embeddings of the pseudo-arc into some spaces (Alejandro Illanes)	40
The double density spectrum of a topological space $(István Juhász)$	41
Baire-one functions on topological spaces: some recent results and open questions (<i>Olena Karlova</i>)	42
New applications of Ψ -spaces in analysis (<i>Piotr Koszmider</i>)	43
The generic continuum approximated by finite graphs with conflue epimorphisms (<i>Aleksandra Kwiatkowska</i>)	ent 44
Catching sequences with ideals (Alexander Shibakov)	45

Selective properties of products of Fréchet–Urysohn spaces (Lyubomyr Zdomskyy)	46
Contributed talks	47
When is a quasi-uniformly continuous real-valued function on a quasi-uniform space bounded? (Collins Amburo Agyingi)	48
On the category of probabilistic topological convergence groups (<i>T. M. G. Ahsanullah</i>)	49
On completeness and topologizability of countable semigroups (Serhii Bardyla)	50
Hereditarily indecomposable continua as Fraïssé limits $(Adam \ Bartoš)$	51
Scattered P-spaces of weight ω_1 (<i>Wojciech Bielas</i>)	52
Some formulas for uniform spaces (Altai Borubaev)	53
A proof of the Tree Alternative Conjecture for the Topological M Relation (Jorge Bruno)	inor 54
On the existence of isovariant extensors for actions of locally com	pact
groups (Alexander Bykov)	55
On the cardinality of a power homogeneous compactum $(Nathan \ Carlson)$	56
Generalized Ważewski dendrites as projective Fraïssé limits (Alessandro Codenotti)	57
Characterization of (semi-)Eberlein compacta using retractional skeletons	
(Marek Cúth)	58
Generating subgroups of the circle using density functions (<i>Pratulananda Das</i>)	59

Embedding of the Higson compactification into the product of adel solenoids	lic
(Alexander Dranishnikov)	60
Planar absolute retracts and countable structures $(Jan \ Dud\acute{a}k)$	61
Separable reductions, rich families and projectional skeletons in non-separable Banach spaces (Marián Fabian)	62
Box and nabla products that are <i>D</i> -spaces (<i>Paul Gartside</i>)	63
Universal flows revisited (Stefan Geschke)	64
On some relative versions of Menger and Hurewicz properties (Davide Giacopello)	65
On some results about cardinal inequalities for topological spaces $(Ivan \ S. \ Gotchev)$	66
Closure spaces, countable conditions and the axiom of choice (Gonçalo Gutierres)	67
A Banach space $C(K)$ reading the dimension of K (<i>Damian Glodkowski</i>)	68
Digital-topological k -group structures on digital objects (Sang-Eon Han)	69
Ramsey theorem for trees with successor operation $(Jan \ Hubička)$	70
Periodicity of solenoidal automorphisms (<i>Faiz Imam</i>)	71
On σ -metacompact function spaces (<i>Heikki Junnila</i>)	72
Topologies related to (I)-envelopes (Ondřej F. K. Kalenda)	73
Selections principles in uniform topology $(Bekbolot \ E. \ Kanetov)$	74

On μ -completeness of uniform spaces and uniformly continuous mappings	
(Dinara E. Kanetova)	75
On a generalization of the selection theorem for C -spaces (<i>Dzmitry Kazhamiakin</i>)	76
Tame locally convex spaces (Matan Komisarchik)	77
Big Ramsey degrees and infinite languages $(Mat\check{e}j \ Kone\check{c}n\hat{y})$	78
Recognizing the topologies on subspaces of L^p -spaces on metric measure spaces (<i>Katsuhisa Koshino</i>)	79
Arbitrarily large countably compact free Abelian groups (Matheus Koveroff Bellini)	80
The Menger property is <i>l</i> -invariant (<i>Mikołaj Krupski</i>)	81
Δ -spaces X and distinguished spaces $C_p(X)$ (Arkady Leiderman)	82
Some compact-type and Lindelöf-type relative versions of star-covering properties (Fortunato Maesano)	83
Descriptive complexity in number theory and dynamics (<i>Bill Mance</i>)	84
On zero-dimensional subspaces of Eberlein compacta and a characterization of ω -Corson compacta (<i>Witold Marciszewski</i>)	85
Orderable groups and semigroup compactifications (Michael Megrelishvili)	86
On the additivity of strong homology for locally compact second countable spaces (Justin Moore)	87
Some topological properties of the N_{τ}^{φ} -nucleus of a space X (Farkhod G. Mukhamadiev)	88

The pseudo-means of the pseudo-arc $(Emanuel R. Márquez)$	89
On uniform real complete spaces (<i>Guliza Namazova</i>)	90
ZFC solution to 9 problems of Tkachuk on functional countability (Peter Nyikos)	91
On entropies in quasi-metric spaces (Olivier Olela Otafudu)	92
Continuity with or without ideal $(Aleksandar Pavlović)$	93
Minimal non-trivial closed hereditary coreflective subcategories in categories of topological spaces	
(Veronika Pitrová)	94
The topological end space problem $(Max \ Pitz)$	95
Ideal boundedness of series vs Banach spaces possessing a copy of (Michał Popławski)	$c_0 \\ 96$
Big Ramsey degrees in the metric context $(No\acute{e} \ de \ Rancourt)$	97
Continuity in right semitopological groups and semineighbourhood the diagonal	s of
(Evgenii Reznichenko)	98
An Asplund space with norming M-basis that is not WCG $(Tommaso Russo)$	99
The properties of tightness type of space of the permutation degree $(Anvar \ K. \ Sadullaev)$	e 100
Weak [*] derived sets (Zdeněk Silber)	101
Čech and Katětov covering dimensions and more or less related questions concerning F -groups	
	102

Cook continua as a tool in topological dynamics	
(Eubomír Snoha)	103
Structure of groups of order-preserving homeomorphisms of produ spaces with lexicographic order and their compactifications (<i>Boris Sorin</i>)	.ct 104
Countable tightness and the Grothendieck property in $C_p(X)$; oth recent results (<i>Franklin D. Tall</i>)	er 105
Some pseudocompact-like properties in certain topological groups $(Juliane\ Trianon-Fraga)$	106
On a new problem of complexity theory arising from Galois–Tukey connections (<i>Peter Vojtáš</i>)	y 107
On sequentiality of Polish topologies (Jindřich Zapletal)	108
An embedded circle into \mathbb{R}^3 might not be able to escape before an isotoped linked circle (Andreas Zastrow)	109
The large-scale geometry of LCA groups (<i>Nicolò Zava</i>)	110
On convex structures in quasi metric spaces (Mcedisi Sphiwe Zweni)	111
Posters	113
Convex realizations of neural codes in one dimension (Karthika Arumugam)	114
Projections of almost connected groups as G-fibrations (Aura Lucina Kantun-Montiel)	115
On dense sets of products of spaces (Anatoly Gryzlov)	116
Index	117

On dense sets of products of spaces

Anatoly Gryzlov¹

gryzlov@udsu.ru

The classical Hewitt–Marczewski–Pondiczery theorem states that if $d(X_s) \leq \tau \ (\omega \leq \tau)$ for every $s \in S$ and $|S| \leq 2^{\tau}$ then $d(\prod_{s \in S} X_s) \leq \tau$. Very important is the problem of the existence of a dense set of a cardinality τ in the product $\prod_{s \in S} X_s$ which contains no convergent nontrivial sequences.

For $\tau = \omega$ the existence of such set were proved for $I^{\mathfrak{c}}$ (W.H. Priestly, 1970), for $D^{\mathfrak{c}}$, where D is the two point discrete space (P. Simon, 1978), for $Z^{\mathfrak{c}}$, where Z is separable not single point T_1 -space (A. Gryzlov, 2018), for a product of $2^{\mathfrak{c}}$ separable decomposable spaces, i.e. spaces, which contain two not empty closed disjoint sets (A. Gryzlov, 2020).

We prove

Theorem. For a regular cardinal τ the product $\prod_{\alpha \in 2^{\tau}} X_{\alpha}$ of decomposable spaces, where $d(X_{\alpha}) = \tau$ ($\alpha \in 2^{\tau}$), contains a dense set Q, $|Q| = \tau$, such that in every subset $P \subseteq Q$, $|P| = \tau$, there is $P' \subseteq P$, $|P'| = \tau$, which contains no convergent nontrivial sequences and therefore is sequentially closed.

¹This work carried within the framework of state assignment of Ministry of Science and Higher Education of Russia (FEWS-2020-0009).

INDEX

Agyingi, Collins Amburo	48
Ahsanullah, T M G	49
Antonyan, Sergey	34
ARUMUGAM, Karthika	114
AVILES, Antonio	35
BANAKH, Taras	20
BARDYLA, Serhii	50
Bartoš, Adam	51
BARTOŠOVÁ, Dana	36
BIELAS, Wojciech	52
Borubaev, Altai	53
BRIAN, Will	37
Bruno, Jorge	54
BYKOV, Alexander	55
CARLSON, Nathan	56
CODENOTTI, Alessandro	57
CÚTH, Marek	58
DAS, Pratulananda	59
Dikranjan, Dikran	38
Dow, Alan	21
DRANISHNIKOV, Alexander	60
Dudák, Jan	61
FABIAN, Marián	62
GARTSIDE, Paul	63
GESCHKE, Stefan	64
GIACOPELLO, Davide	65
Glasner, Eli	22
Gotchev, Ivan	66
Gryzlov, Anatoly	116
GUTIERRES, Gonçalo	67
GLODKOWSKI, Damian	68
HAN, Sang-Eon	69
HERNANDEZ-GUTIERREZ, Rodrigo	39
HRUSAK, Michael	23
HUBIČKA, Jan	70

ILLANES, Alejandro	40
IMAM, Faiz	71
Juhász, István	41
JUNNILA, Heikki	72
Kalenda, Ondřej	73
KANETOV, Bekbolot	74
KANETOVA, Dinara	75
KANTUN-MONTIEL, Aura Lucina	115
KARLOVA, Olena	42
KAZHAMIAKIN, Dzmitry	76
Komisarchik, Matan	77
Konečný, Matěj	78
Koshino, Katsuhisa	79
Koszmider, Piotr	43
KOVEROFF BELLINI, Matheus	80
KRUPSKI, Mikołaj	81
Kurka, Ondřej	24
KWIATKOWSKA, Aleksandra	44
Leiderman, Arkady	82
Maesano, Fortunato	83
MANCE, Bill	84
Marciszewski, Witold	85
MEGRELISHVILI, Michael	86
van Mill, Jan	25
MOORE, Justin	87
Mukhamadiev, Farkhod	88
MÁRQUEZ, Emanuel R.	89
NAMAZOVA, Guliza	90
Nyikos, Peter	91
Olela Otafudu, Olivier	92
OPROCHA, Piotr	26
PAVLOVIĆ, Aleksanar	93
PESTOV, Vladimir	27
PITROVÁ, Veronika	94
PITZ, Max	95

Popławski, Michał	96
de Rancourt, Noé	97
REZNICHENKO, Evgenii	98
ROSENDAL, Christian	28
Russo, Tommaso	99
SADULLAEV, Anvar	100
SHIBAKOV, Alexander	45
SILBER, Zdeněk	101
SIPACHEVA, Olga	102
SNOHA, Ľubomír	103
SORIN, Boris	104
TALL, Franklin	105
TKACHENKO, Mikhail	29
TODORCEVIC, Stevo	30
TRIANON-FRAGA, Juliane	106
TSABAN, Boaz	31
Vojtas, Peter	107
ZAPLETAL, Jindrich	108
ZASTROW, Andreas	109
ZAVA, Nicolò	110
ZDOMSKYY, Lyubomyr	46
ZWENI, Mcedisi	111

Торозум 2022 – Воок оf Abstracts A. Bartoš, D. Chodounský (eds.)

Printed by Reprostředisko MFF UK for the Thirteenth Symposium on General Topology and its Relations to Modern Analysis and Algebra, which took place in Prague, 25–29 July 2022. Published by Matfyzpress, the publishing house of the Faculty of Mathematics and Physics of the Charles University. Design based on Toposym 2016 Book of Abstracts by J. Verner. Typeset with T_EX. Prague 2022.